

2016 International Perforating Symposium (IPS)

IPS-16-39

# Plastic Collapse Behaviors of Perforating Guns with Scallops

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Schlumberger  
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# Outline

- I. Introduction to Perforating Gun and Conveyance Systems
- II. Ultimate Collapse Strength for Recessed Tubulars
- III. Finite Element Analysis (FEA) and Test Validation
- IV. Conclusions and Future Work

# I. Introduction to Perforating Gun and Conveyance Systems

# Perforating Gun and Conveyance Systems



Wireline



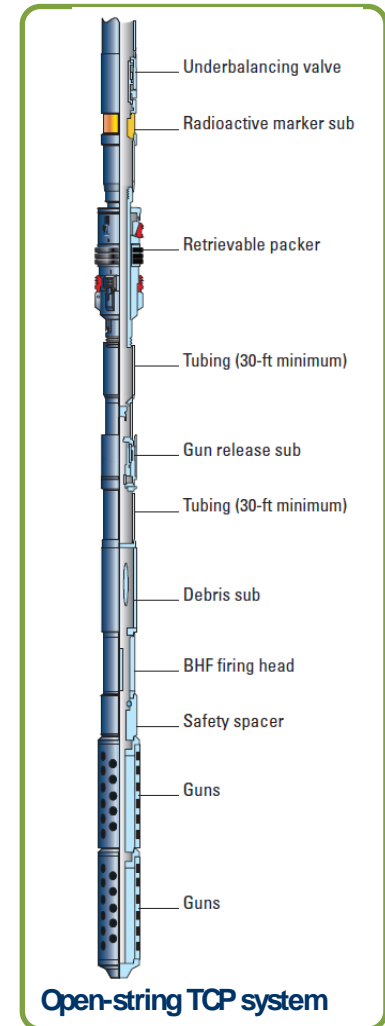
Slickline



Tubing-Conveyed Perforating (TCP):  
Completions and Drillstem testing

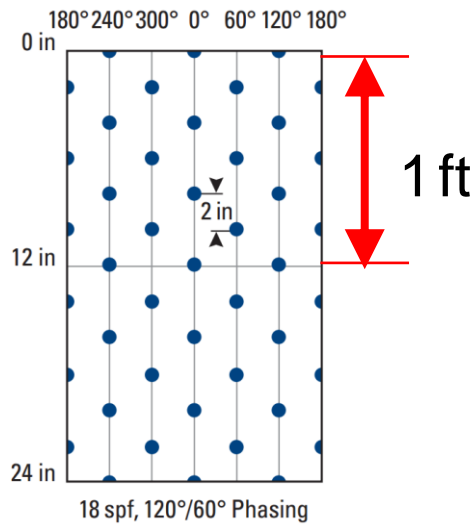
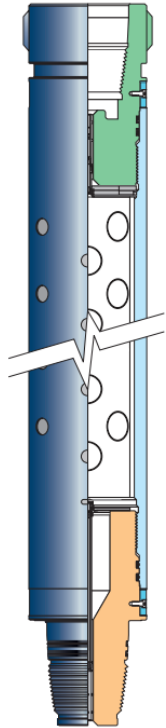


Coiled Tubing



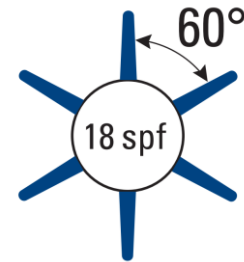
# Density and Phasing

## Density



Number of shots per foot (spf)

## Phasing




$$360^\circ / 6 = 60^\circ \text{ phasing}$$

Distance (in degrees) between charges

## II. Ultimate Collapse Strength for Recessed Tubulars

# Review: Collapse Strength of a Slick Pipe

- **Lamé Thick Wall Yield Collapse Formula (Yield at Pipe ID)**

Open Ends	$P_{Lc} = \sigma_y \frac{D_o^2 - D_i^2}{2D_o^2}$	<div style="border: 1px solid blue; padding: 5px; display: inline-block;"> <math>D_o = D</math>  <math>t = \frac{1}{2}(D_o - D_i)</math>  <math>k = D/t</math> </div> 	$P_{Lc} = 2\sigma_y \cdot \frac{(k-1)}{k^2}$
Closed Ends	$P_{Lc} = \sigma_y \frac{D_o^2 - D_i^2}{\sqrt{3}D_o^2}$		$P_{Lc} = 2.31 \cdot \sigma_y \cdot \frac{(k-1)}{k^2}$

- **API Bulletin 5C3**

Yield Collapse	Plastic Collapse	Transition Collapse	Elastic Collapse
$P_{Ys} = 2\sigma_y \cdot \frac{(k-1)}{k^2}$	$P_P = \sigma_y \left[ \frac{A}{k} - B \right] - C$	$P_T = \sigma_y \left[ \frac{F}{k} - G \right]$	$P_{TE} = \frac{2E}{1-\nu^2} \cdot \frac{1}{k(k-1)^2}$

- **Tamano Ultimate Collapse Equation (SPE 48331)**

$P_T = \frac{1}{2}(P_E + P_Y) - \sqrt{\frac{1}{4}(P_E - P_Y)^2 + P_E P_Y H}$	$\left\{ \begin{array}{l} P_E = 1.08 \times \frac{2E}{1-\nu^2} \cdot \frac{1}{k(k-1)^2} \\ P_Y = 2\sigma_y \cdot \frac{k-1}{k^2} \left[ 1 + \frac{1.5}{k-1} \right] \\ H = 0.071 \cdot u(\%) + 0.0022 \cdot e(\%) - 0.18 \cdot \frac{\sigma_r}{\sigma_y} \end{array} \right.$
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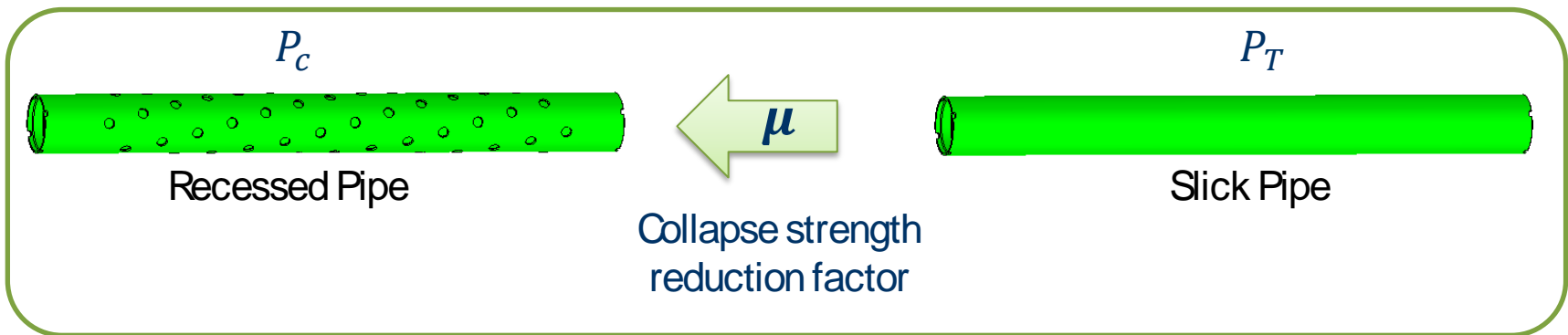
# Ultimate Collapse Strength of Scalloped Gun Carriers

## Definition

$$P_C = \mu \cdot P_T$$

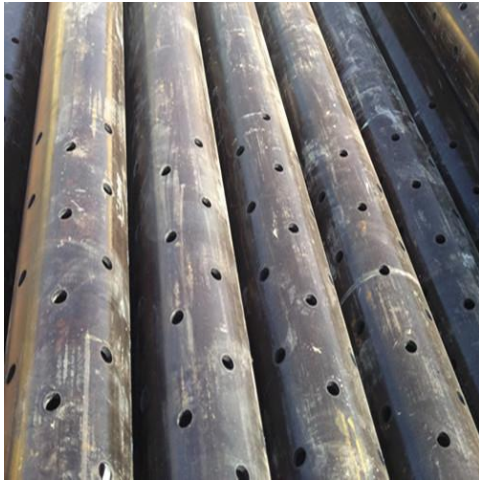
$\mu$  – Collapse strength reduction factor due to scallops

$P_T$  – Tamano ultimate collapse strength equation



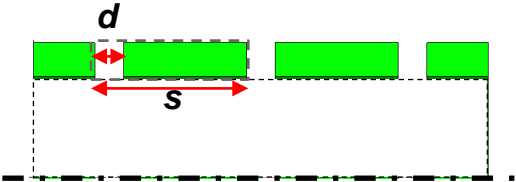


# Reference: Collapse Strength of Perforated Casing

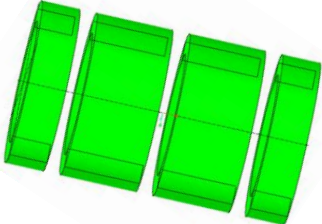


$$\mu_0 = 1 - \frac{d}{S}$$

$d/S$  – (1D) spacing fraction of recess



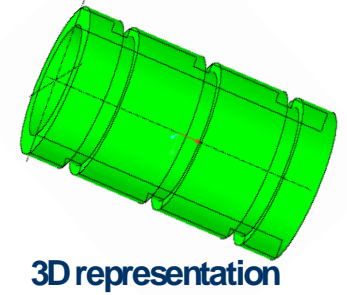
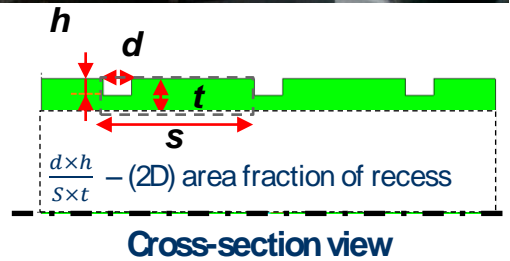
Cross-section view



3D representation

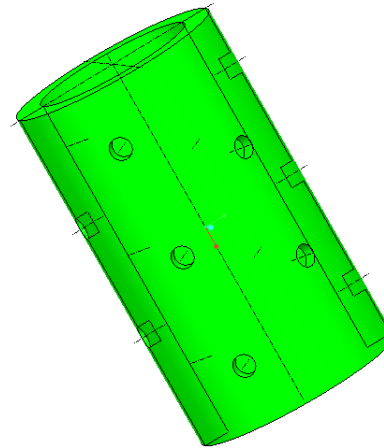
Reference: SPE 51188

# $\mu$ for Scalloped Gun Carriers



- 1  $\mu_1 = 1 - \frac{d}{s} \cdot \frac{h}{t}$
- 2  $\mu_2 = 1 - f_r$
- 3  $\mu_3 = 1 - \alpha f_r$

$f_r$  – (3D) volume fraction of recess  
 $\alpha$  – fitting factor

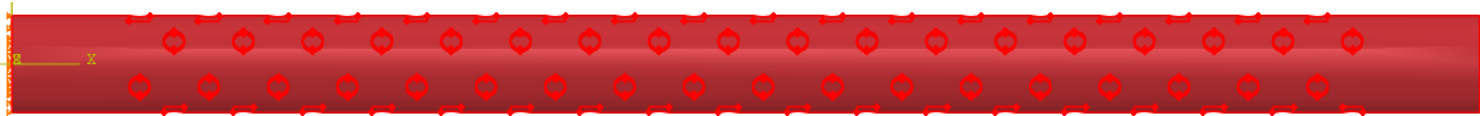
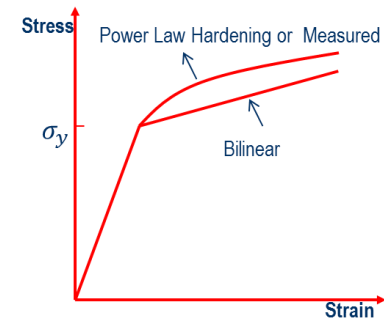


## III. FEA and Test Validation

# Modeling Approach

## Description

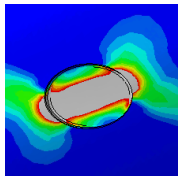
- Nonlinear post-buckling analysis using Riks method based on arc length scheme in ABAQUS
- Material model: isotropic hardening plasticity with bilinear, power law or measured stress-strain curve
- Boundary conditions: external pressure prescribed on the exterior surface with end connection supported



## Collapse Criteria

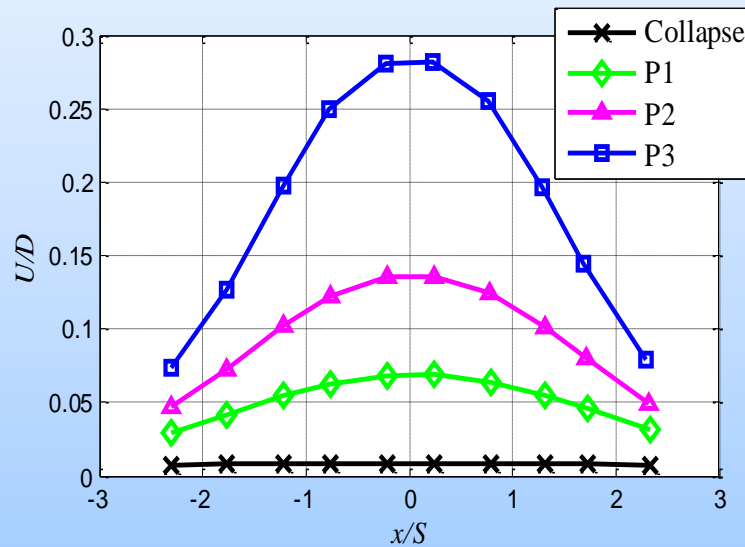
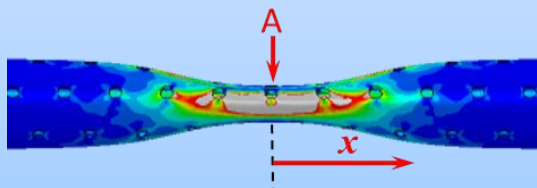
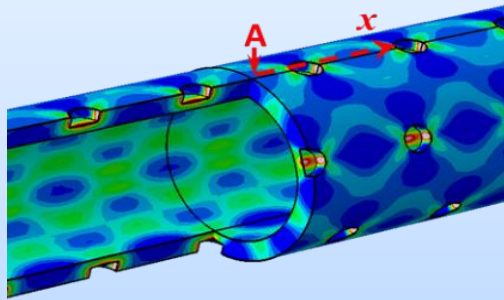
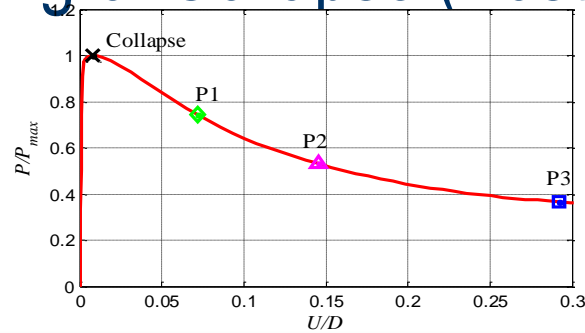
- When the collapse pressure is reached, the structure will deform dramatically and lose pressure-bearing capacity.

## Local Yielding

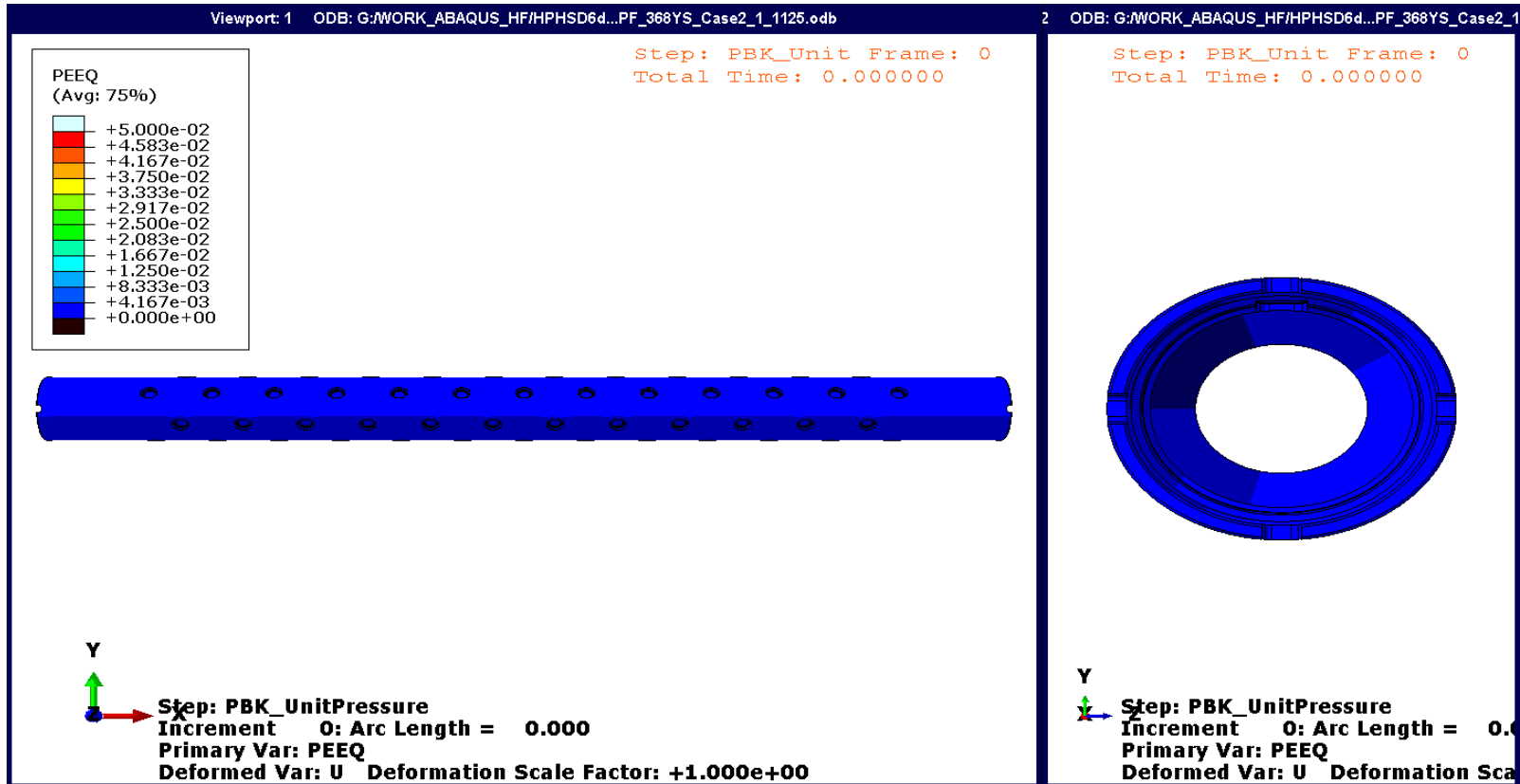


# Physical Understanding of Collapse (Post-buckling)

Collapse pressure definition



# Example: Collapse Animation of 15SPF 5 FT



Deformation Scale Factor = 1

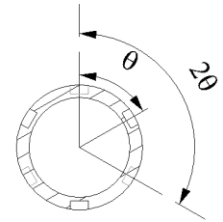
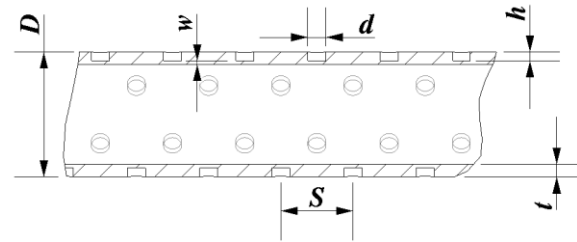
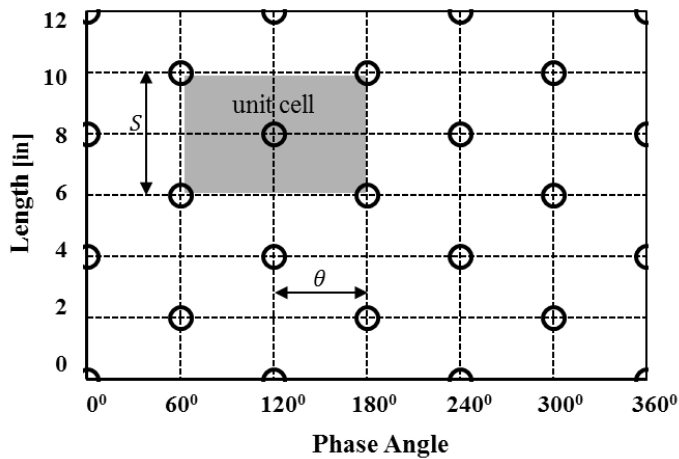
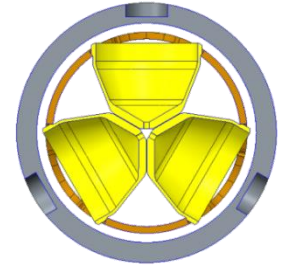
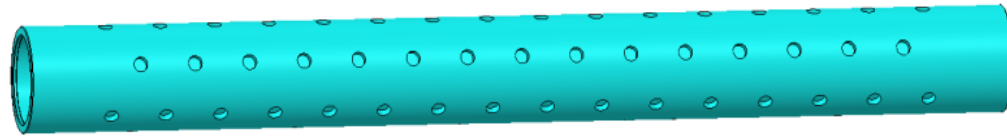
# Test Validation of FEA

Description	Test Temp [Deg F]	D/t	Tested Collapse Pressure [psi]	FEA $P_{collapse}$ [psi]	Difference with Tests [%]
Test 1	368	9.4	32,250	30,660	-4.9%
Test 2	318	10.7	22,500	22,831	+1.5%
Test 3	250	10.7	24,263	23,651	-2.5%
Test 4	250	14.0	18,329	18,633	+1.7%
Test 5	400	11.6	22,745	23,311	+2.4%

Note:

- Detailed geometric, product name and material parameters are confidential.
- Stress/strain data utilized in the FEA analyses is full measured data from a test

# Case Study: $\mu_2$ Expression



$$f_r = V_s / V_u$$

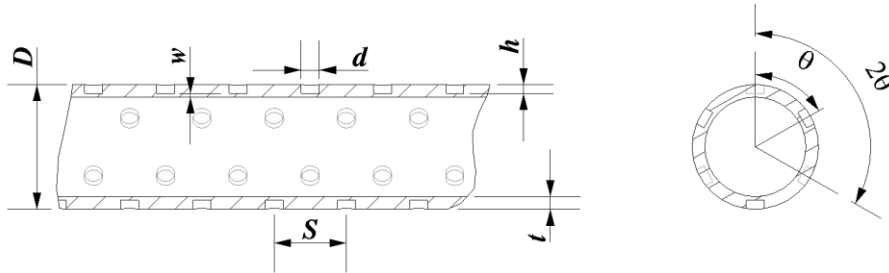
$$V_u = S \times \frac{\pi}{180} \theta D \times t$$

$$V_s = 2 \times \frac{1}{4} \pi d^2 h$$

$$\mu_2 = 1 - f_r = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$



# Case Study: Parametric Study of 7-in OD, 5-ft Length Carrier



## Angular Phasing, $\theta$

D [in]	t [in]	$\theta$ [deg]	S [in]	h [in]	d [in]
7	0.7	25.7	4.0	0.5	1.0
		36			
		45			
		60			
		90			

## Wall Thickness, $t$

D [in]	t [in]	$\theta$ [deg]	S [in]	w [in]	d [in]
7	0.5	60	4.0	0.2	1.0
	0.7				
	1.0				

## Scallop Depth, $h$

D [in]	t [in]	$\theta$ [deg]	S [in]	h [in]	d [in]
7	0.7	60	4.0	0.3	1.0
				0.4	
				0.5	
				0.6	
				0.6	

## Longitudinal Spacing, $S$

D [in]	t [in]	$\theta$ [deg]	S [in]	h [in]	d [in]
7	0.7	60	4.0	0.5	1.0
			6.0		
			8.0		
			12.0		
			16.0		

## Scallop Diameter, $d$

D [in]	t [in]	$\theta$ [deg]	S [in]	h [in]	d [in]
7	0.7	60	4.0	0.5	0.7
					1.0
					1.3

## Definition of “true” $\mu$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

## Dimension of slick pipes

D [in]	t [in]
7	0.5
	0.7
	1.0

# Sensitivity Study of Collapse Strength Reduction Factor

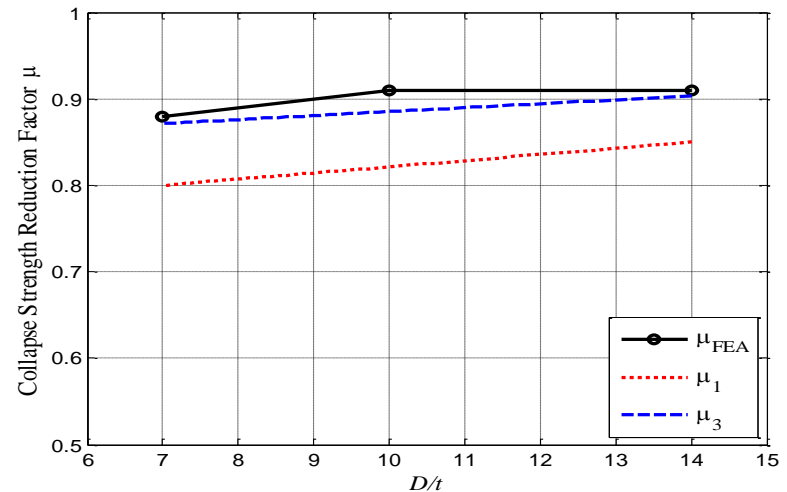
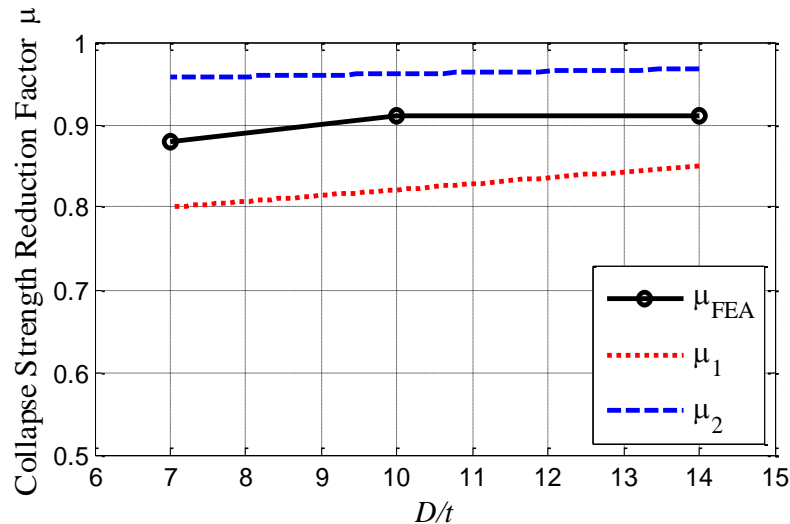
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{FEA} = P_{scallop}^{FEA} / P_{pipe}^{FEA}$$

[1]  $D/t$  vs.  $\mu$



Collapse strength reduction factor  $\mu$  is linearly proportional to  $D/t$  ratio.

# Sensitivity Study of Collapse Strength Reduction Factor

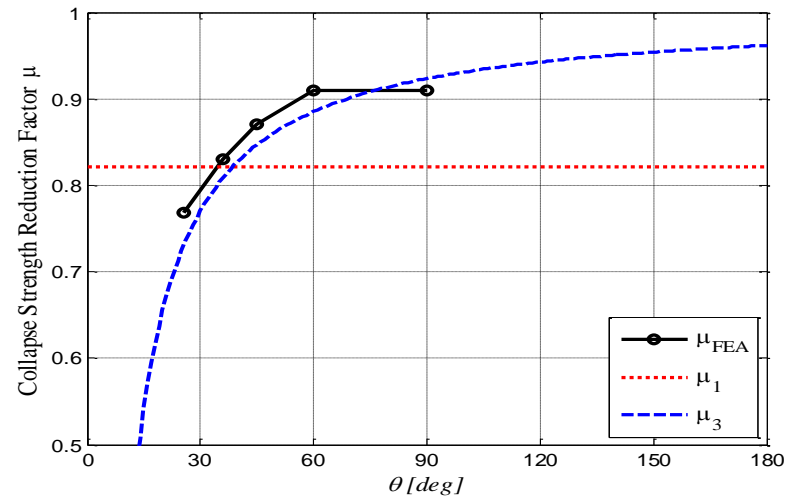
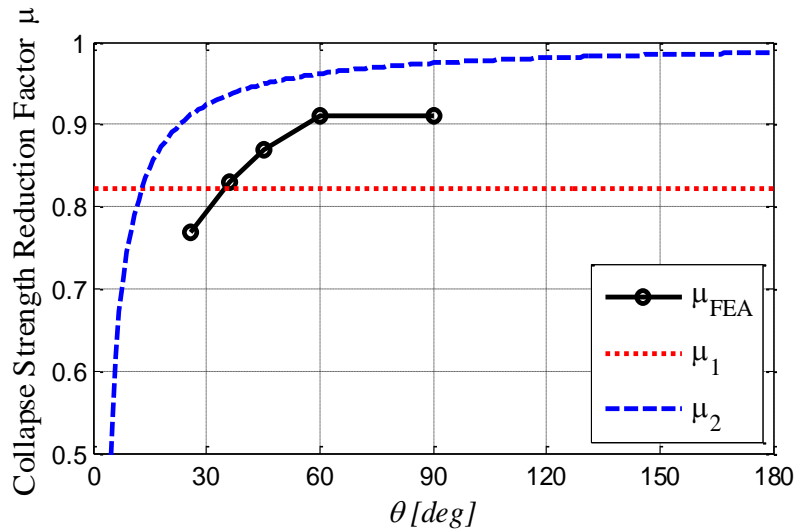
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{FEA} = P_{scallop}^{FEA} / P_{pipe}^{FEA}$$

[2]  $\theta$  vs.  $\mu$



Collapse strength reduction factor  $\mu$  is inversely proportional to  $\theta$ .

# Sensitivity Study of Collapse Strength Reduction Factor

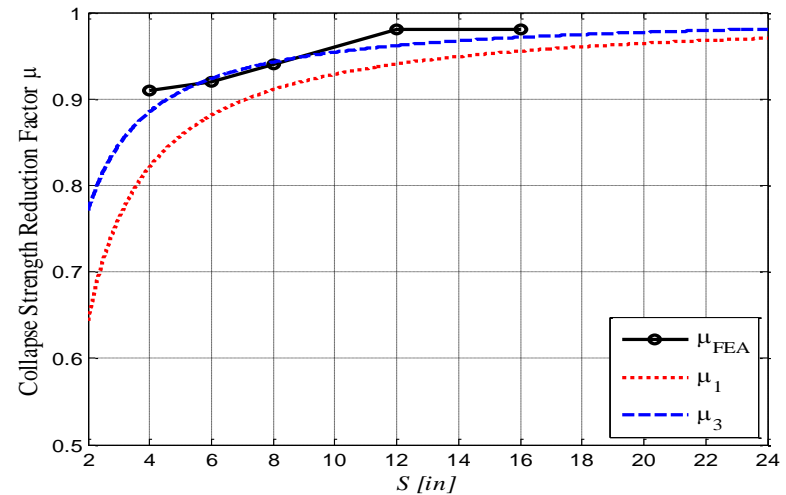
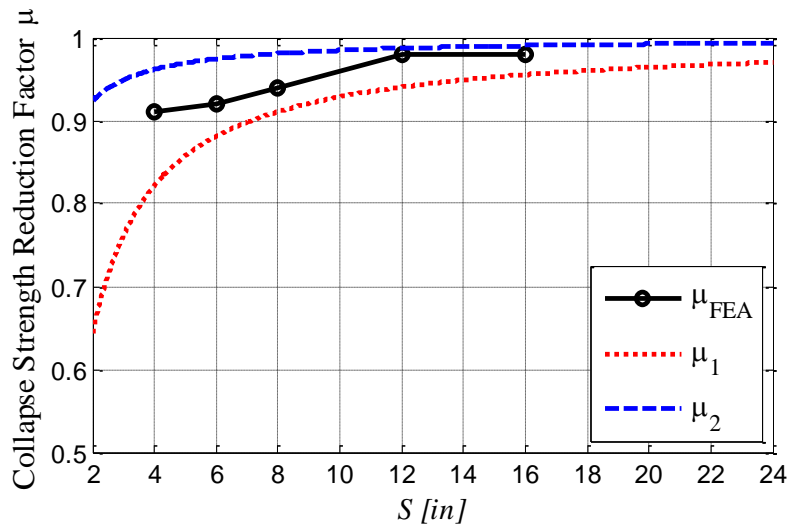
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[3]  $S$  vs.  $\mu$



Collapse strength reduction factor  $\mu$  is inversely proportional to  $S$ .

# Sensitivity Study of Collapse Strength Reduction Factor

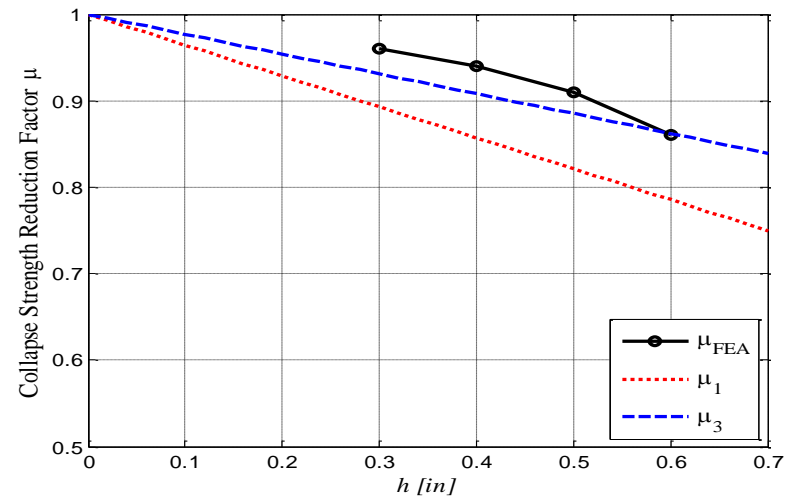
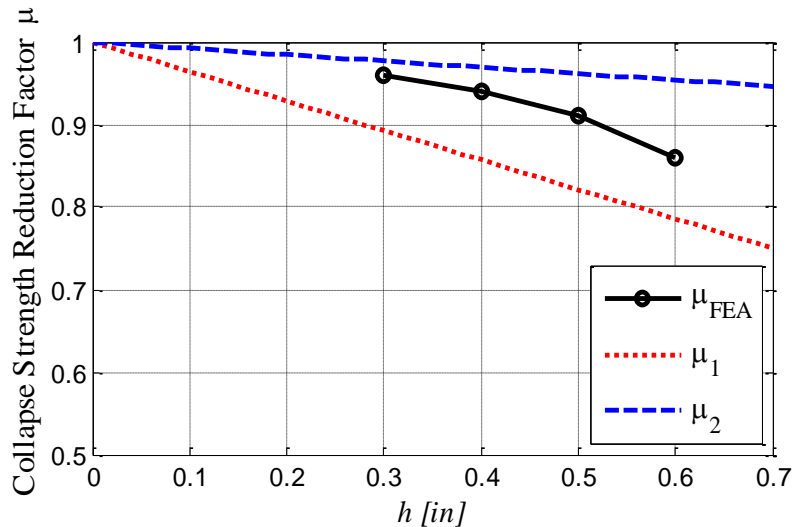
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{FEA} = P_{scallop}^{FEA} / P_{pipe}^{FEA}$$

## [4] $h$ vs. $\mu$



Collapse strength reduction factor  $\mu$  is “linearly” proportional to  $h$ .

# Sensitivity Study of Collapse Strength Reduction Factor

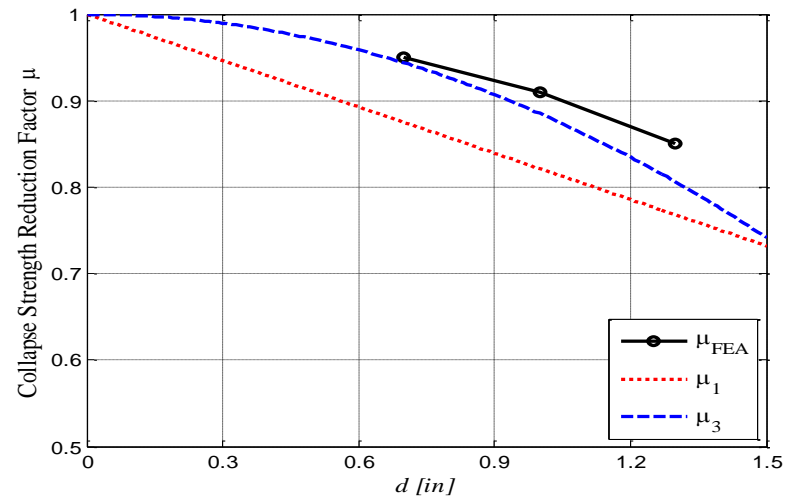
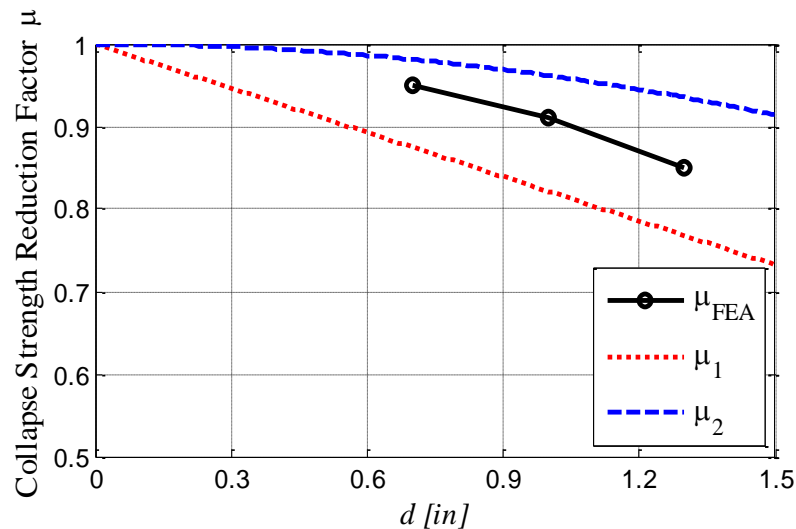
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[5]  $d$  vs.  $\mu$



Collapse strength reduction factor  $\mu$  is a quadratic function of  $d$ .

## IV. Conclusions and Future Work

# Conclusions and Future Work

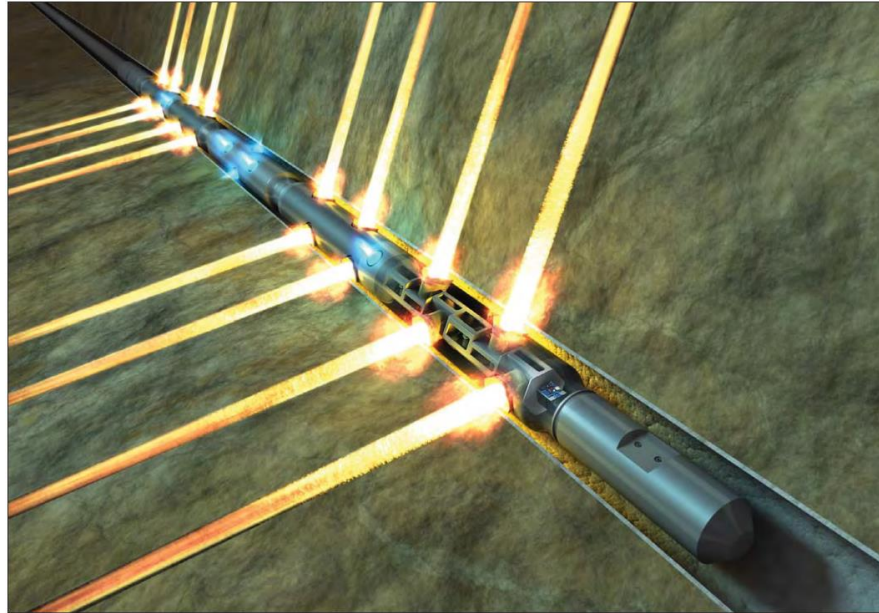
- An analytical collapse strength equation based on Tamano formula was proposed for scalloped perforating guns.
- The proposed equation was thoroughly validated with the aid of FEA in a multivariable parametric space – an analysis hardly affordable with the use of physical tests.
- An FEA method used to validate the proposed equation showed strong agreement with the test data giving collapse predictions for scalloped tubulars within 5% of the test results.
- The method applied to scalloped perforating guns can also be used for any tubulars with patterned cutouts or recesses, such as prepacked sand screens, perforated or slotted liners, etc.





IPS-16-39

# Questions?



## Publications

- Zhao, H., Iblings, D., Barykin, A., and Mehdi, M., 2015, Plastic Collapse Behaviors of Tubulars with Recess Patterns, Proceedings of ASME International Mechanical Engineering Congress & Exposition, IMECE2015-50204, Houston, TX.
- Zhao, H., Iblings, D., Barykin, A., and Mehdi, M., 2016, Plastic Collapse Behaviors of Tubulars with Recess Patterns, ASCE-ASME Journal of Risk and Uncertainty in Engineering Systems, Part B: Mechanical Engineering , Accepted.