



2016 International Perforating Symposium (IPS)

IPS-16-39

Plastic Collapse Behaviors of Perforating Guns with Scallops

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Schlumberger
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Outline

- I. Introduction to Perforating Gun and Conveyance Systems
- II. Ultimate Collapse Strength for Recessed Tubulars
- III. Finite Element Analysis (FEA) and Test Validation
- IV. Conclusions and Future Work

I. Introduction to Perforating Gun and Conveyance Systems

Perforating Gun and Conveyance Systems



Wireline



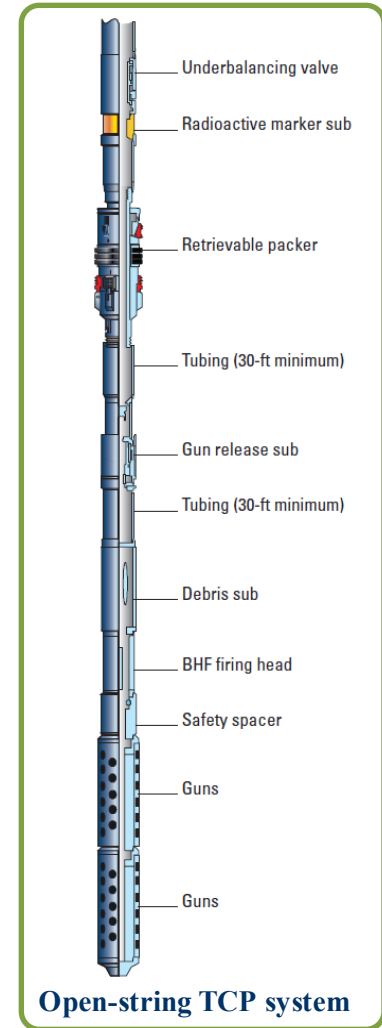
Tubing-Conveyed Perforating (TCP):
Completions and Drillstem testing



Slickline

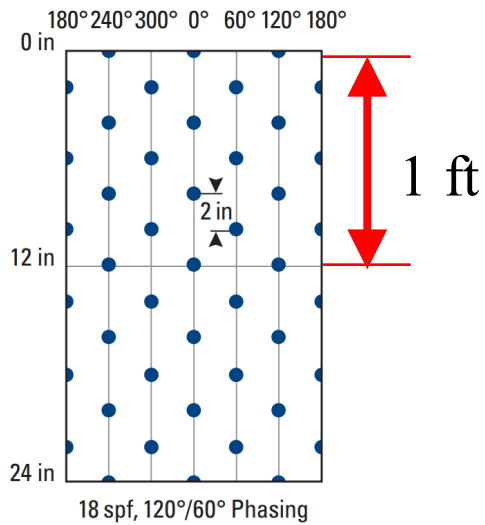
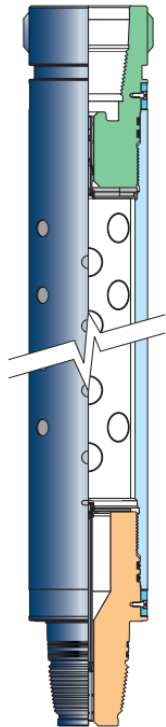


Coiled Tubing



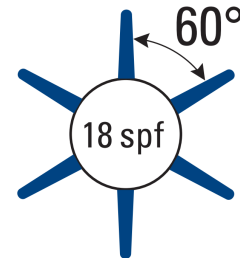
Density and Phasing

Density



Number of shots per foot (spf)

Phasing




$360^\circ / 6 = 60^\circ$ phasing

Distance (in degrees) between charges

II. Ultimate Collapse Strength for Recessed Tubulars

Review: Collapse Strength of a Slick Pipe

- **Lamé Thick Wall Yield Collapse Formula (Yield at Pipe ID)**

Open Ends	$P_{Lc} = \sigma_y \frac{D_o^2 - D_i^2}{2D_o^2}$	<div style="border: 1px solid blue; padding: 5px; display: inline-block;"> $D_o = D$ $t = \frac{1}{2}(D_o - D_i)$ $k = D/t$ </div> 	$P_{Lc} = 2\sigma_y \cdot \frac{(k-1)}{k^2}$
Closed Ends	$P_{Lc} = \sigma_y \frac{D_o^2 - D_i^2}{\sqrt{3}D_o^2}$		$P_{Lc} = 2.31 \cdot \sigma_y \cdot \frac{(k-1)}{k^2}$

- **API Bulletin 5C3**

Yield Collapse	Plastic Collapse	Transition Collapse	Elastic Collapse
$P_{Ys} = 2\sigma_y \cdot \frac{(k-1)}{k^2}$	$P_P = \sigma_y \left[\frac{A}{k} - B \right] - C$	$P_T = \sigma_y \left[\frac{F}{k} - G \right]$	$P_{TE} = \frac{2E}{1-\nu^2} \cdot \frac{1}{k(k-1)^2}$

- **Tamano Ultimate Collapse Equation (SPE 48331)**

$P_T = \frac{1}{2}(P_E + P_Y) - \sqrt{\frac{1}{4}(P_E - P_Y)^2 + P_E P_Y H}$	$\left\{ \begin{array}{l} P_E = 1.08 \times \frac{2E}{1-\nu^2} \cdot \frac{1}{k(k-1)^2} \\ P_Y = 2\sigma_y \cdot \frac{k-1}{k^2} \left[1 + \frac{1.5}{k-1} \right] \\ H = 0.071 \cdot u(\%) + 0.0022 \cdot e(\%) - 0.18 \cdot \frac{\sigma_r}{\sigma_y} \end{array} \right.$
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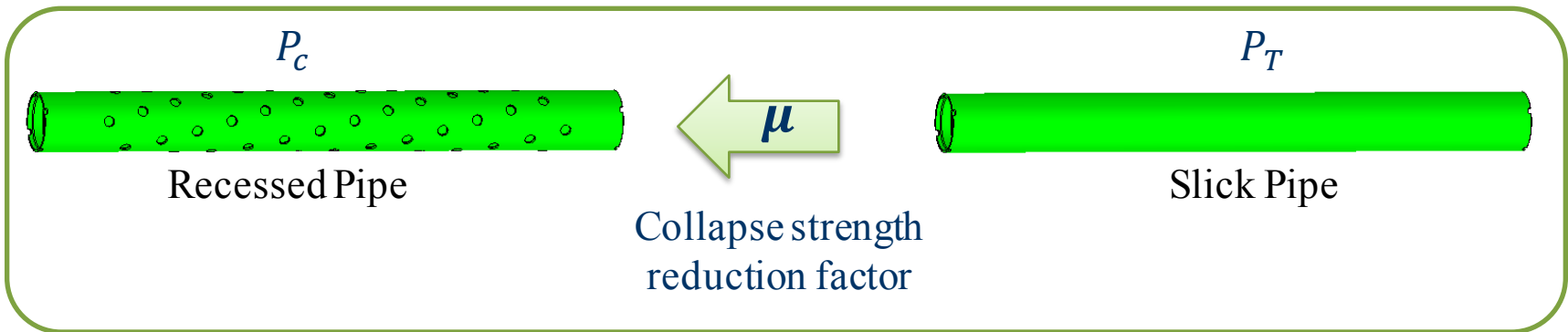
Ultimate Collapse Strength of Scalloped Gun Carriers

Definition

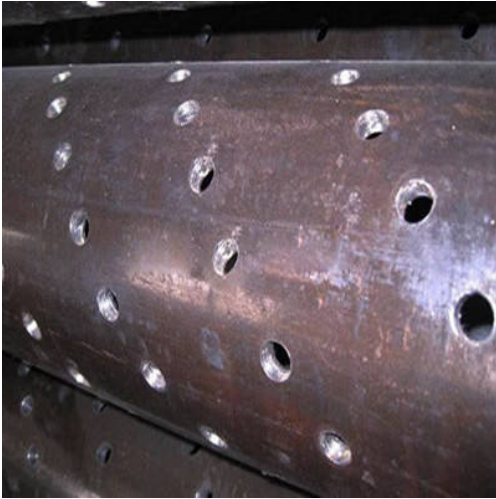
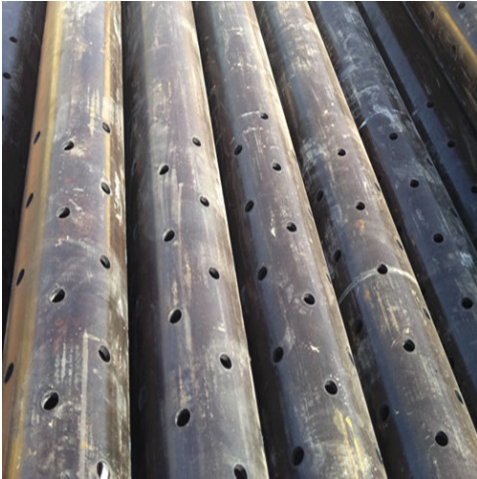
$$P_C = \mu \cdot P_T$$

μ – Collapse strength reduction factor due to scallops

P_T – Tamano ultimate collapse strength equation

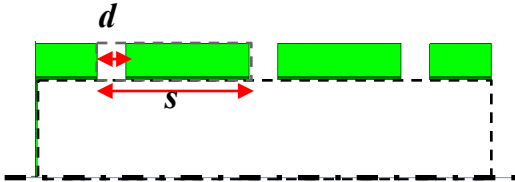


Reference: Collapse Strength of Perforated Casing

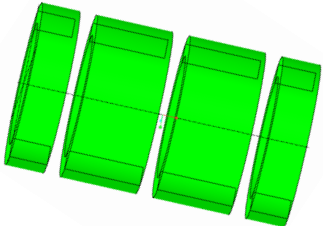


$$\mu_0 = 1 - \frac{d}{S}$$

d/S – (1D) spacing fraction of recess



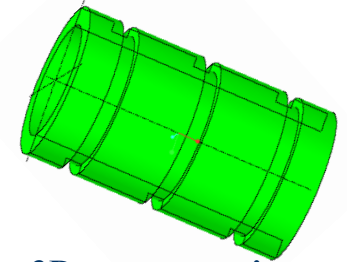
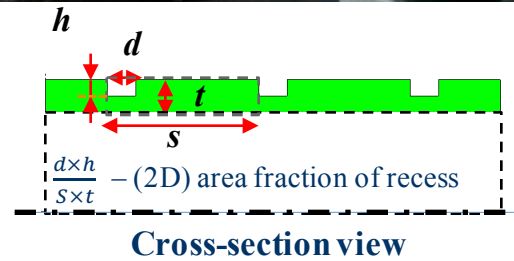
Cross-section view



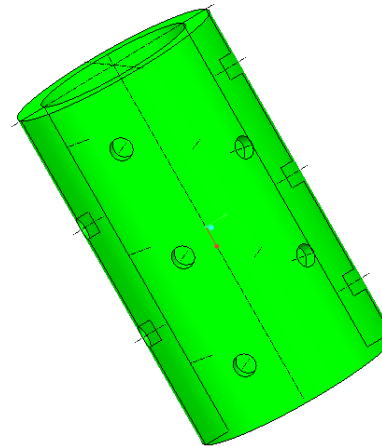
3D representation

Reference: SPE 51188

μ for Scalloped Gun Carriers



3D representation



- 1 $\mu_1 = 1 - \frac{d}{s} \cdot \frac{h}{t}$
- 2 $\mu_2 = 1 - f_r$
- 3 $\mu_3 = 1 - \alpha f_r$

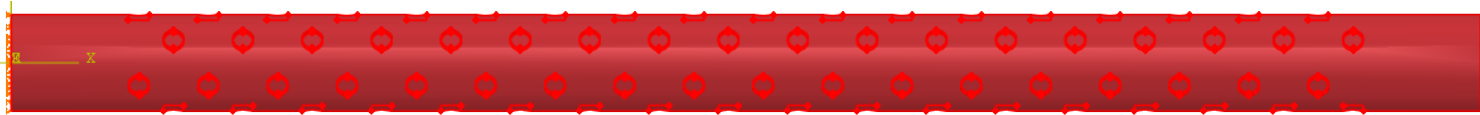
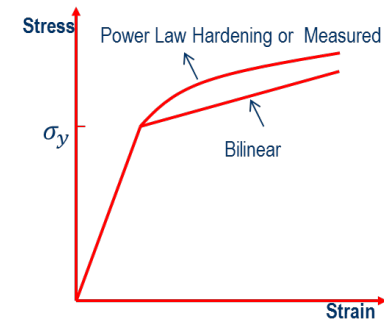
f_r – (3D) volume fraction of recess
 α – fitting factor

III. FEA and Test Validation

Modeling Approach

Description

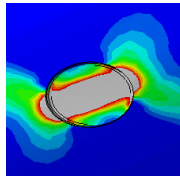
- Nonlinear post-buckling analysis using Riks method based on arc length scheme in ABAQUS
- Material model: isotropic hardening plasticity with bilinear, power law or measured stress-strain curve
- Boundary conditions: external pressure prescribed on the exterior surface with end connection supported



Collapse Criteria

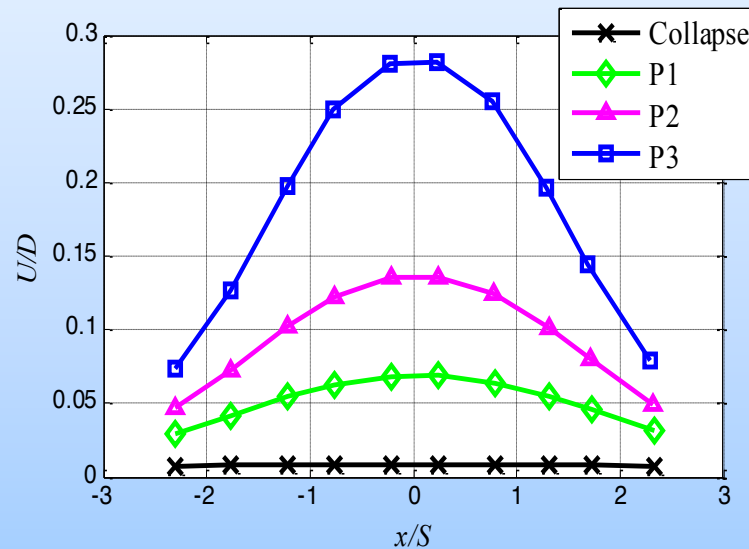
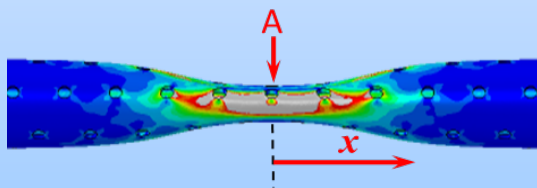
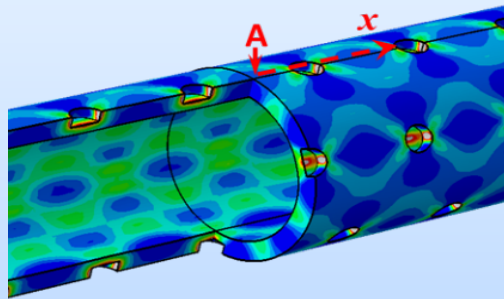
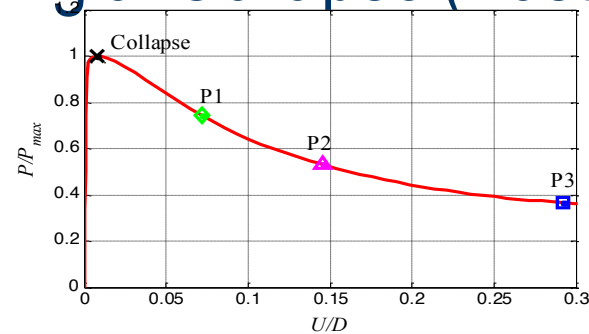
- When the collapse pressure is reached, the structure will deform dramatically and lose pressure-bearing capacity.

Local Yielding

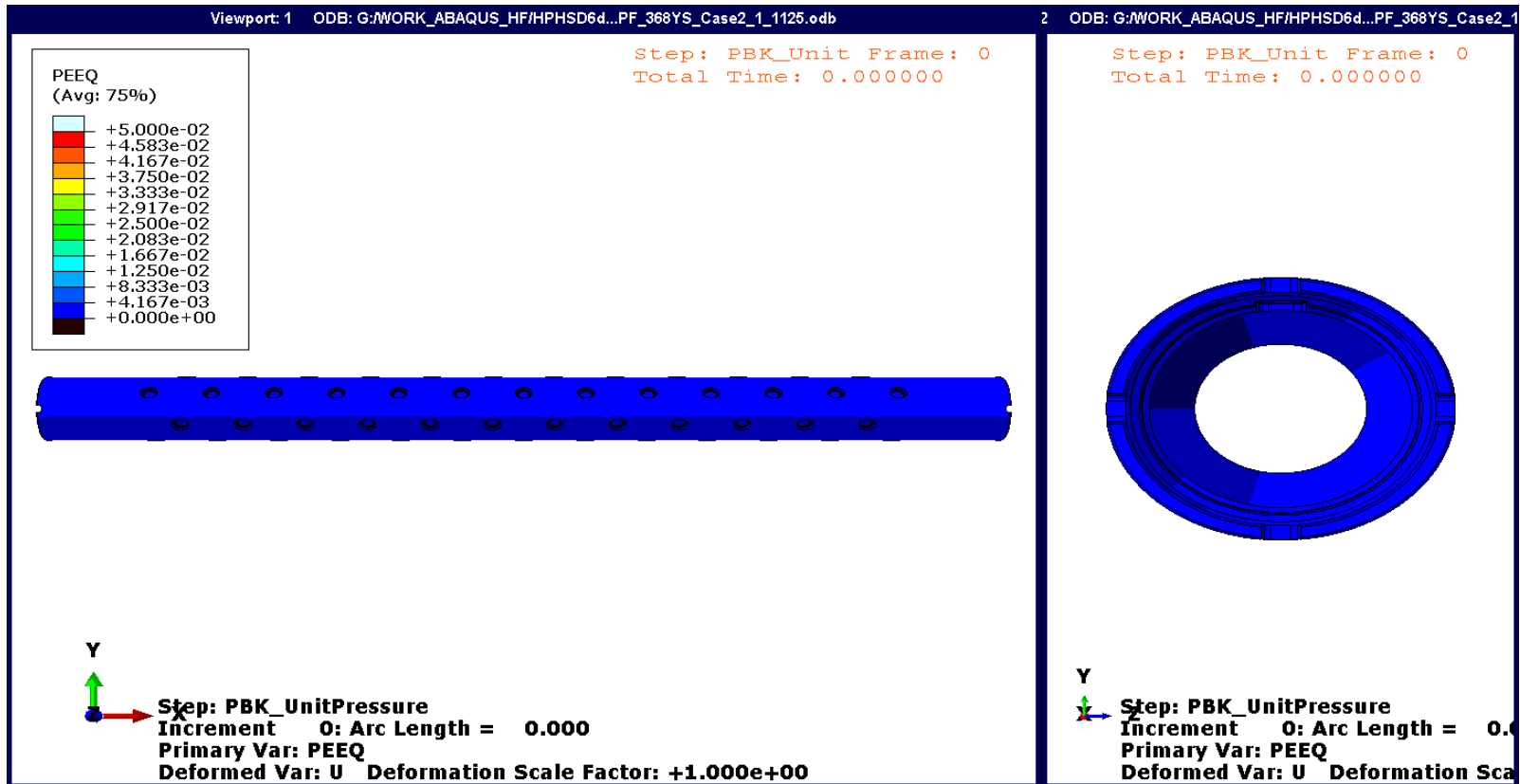


Physical Understanding of Collapse (Post-buckling)

Collapse pressure definition



Example: Collapse Animation of 15SPF 5 FT



Deformation Scale Factor = 1

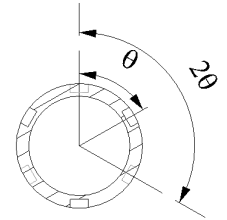
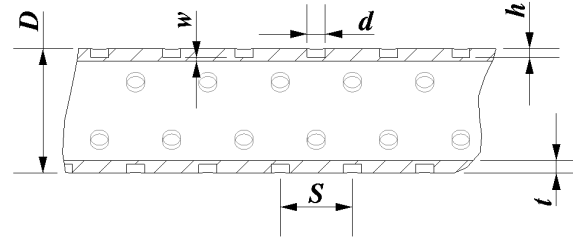
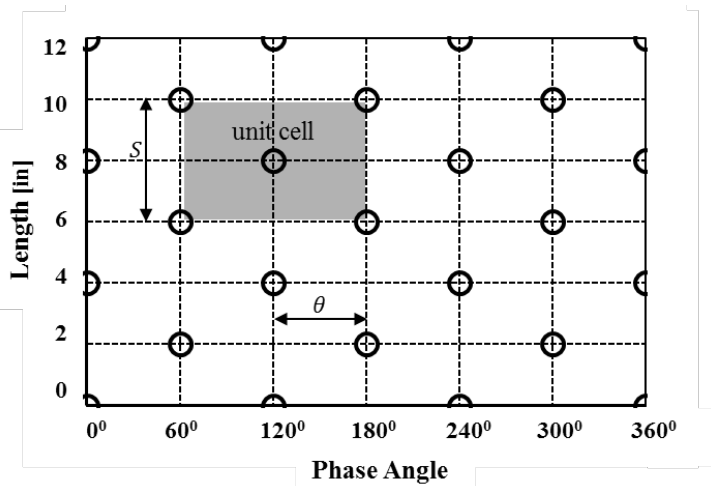
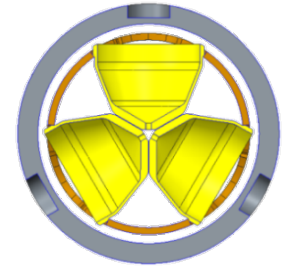
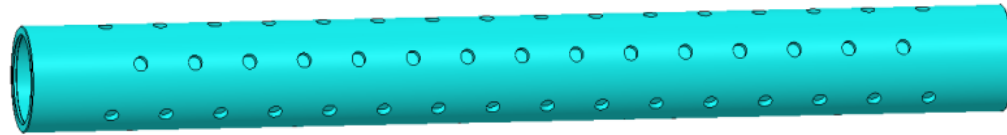
Test Validation of FEA

Description	Test Temp [Deg F]	D/t	Tested Collapse Pressure [psi]	FEA $P_{collapse}$ [psi]	Difference with Tests [%]
Test 1	368	9.4	32,250	30,660	-4.9%
Test 2	318	10.7	22,500	22,831	+1.5%
Test 3	250	10.7	24,263	23,651	-2.5%
Test 4	250	14.0	18,329	18,633	+1.7%
Test 5	400	11.6	22,745	23,311	+2.4%

Note:

- Detailed geometric, product name and material parameters are confidential.
- Stress/strain data utilized in the FEA analyses is full measured data from a test

Case Study: μ_2 Expression



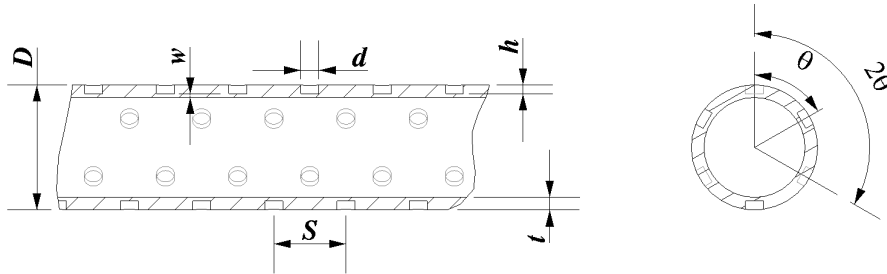
$$f_r = V_s/V_u$$

$$V_u = S \times \frac{\pi}{180} \theta D \times t$$

$$V_s = 2 \times \frac{1}{4} \pi d^2 h$$

$$\mu_2 = 1 - f_r = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

Case Study: Parametric Study of 7-in OD, 5-ft Length Carrier



Angular Phasing, θ

D [in]	t [in]	θ [deg]	S [in]	h [in]	d [in]
7	0.7	25.7	4.0	0.5	1.0
		36			
		45			
		60			
		90			

Wall Thickness, t

D [in]	t [in]	θ [deg]	S [in]	w [in]	d [in]
7	0.5	60	4.0	0.2	1.0
	0.7				
	1.0				

Scallop Depth, h

D [in]	t [in]	θ [deg]	S [in]	h [in]	d [in]
7	0.7	60	4.0	0.3	1.0
				0.4	
				0.5	
				0.5	
				0.6	

Longitudinal Spacing, S

D [in]	t [in]	θ [deg]	S [in]	h [in]	d [in]
7	0.7	60	4.0	0.5	1.0
			6.0		
			8.0		
			12.0		
			12.0		
			16.0		

Scallop Diameter, d

D [in]	t [in]	θ [deg]	S [in]	h [in]	d [in]
7	0.7	60	4.0	0.5	0.7
					1.0
					1.3

Definition of “true” μ

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

Dimension of slick pipes

D [in]	t [in]
7	0.5
	0.7
	1.0

Sensitivity Study of Collapse Strength Reduction Factor

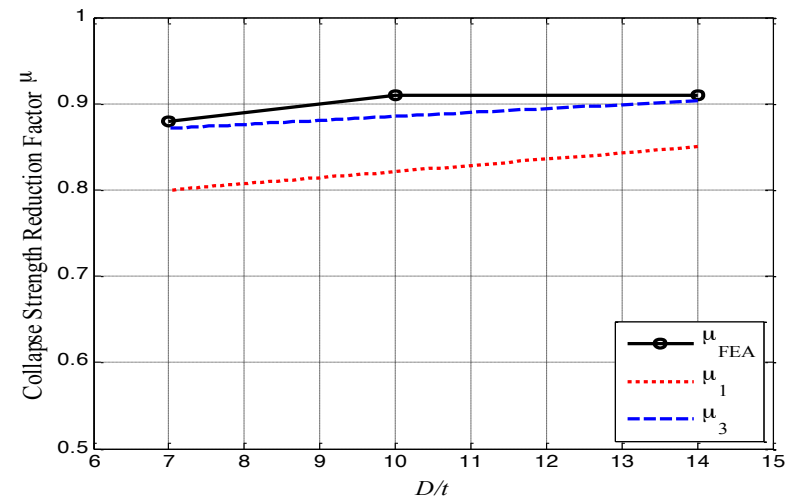
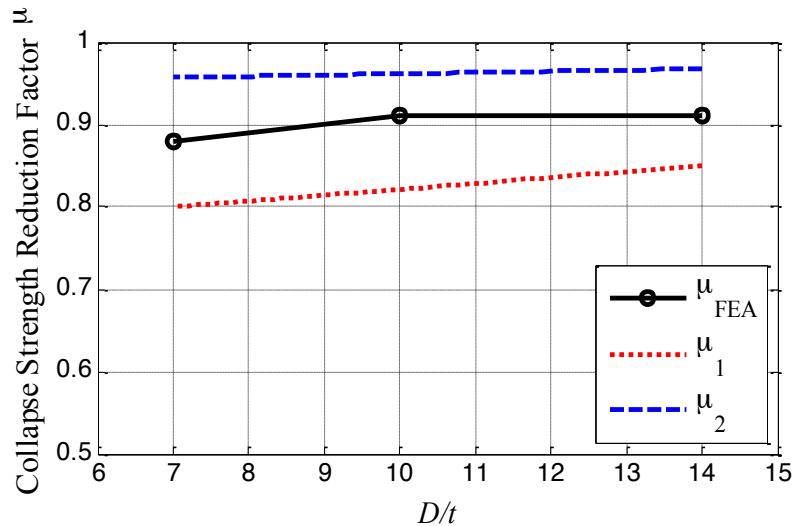
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[1] D/t vs. μ



Collapse strength reduction factor μ is linearly proportional to D/t ratio.

Sensitivity Study of Collapse Strength Reduction Factor

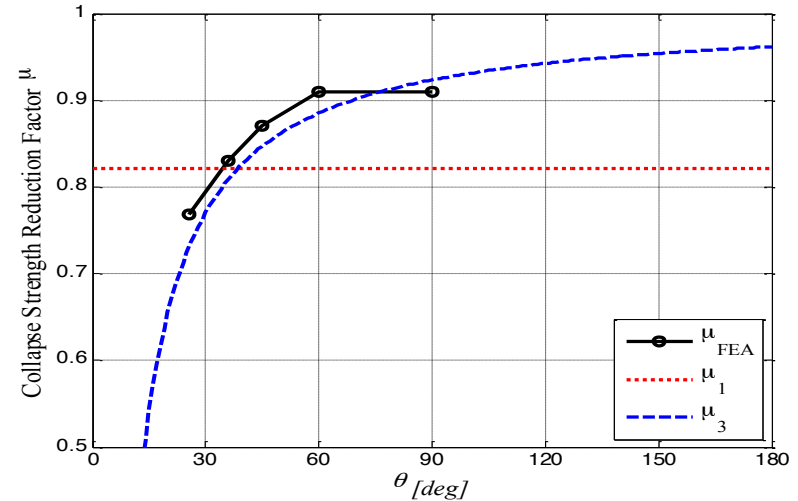
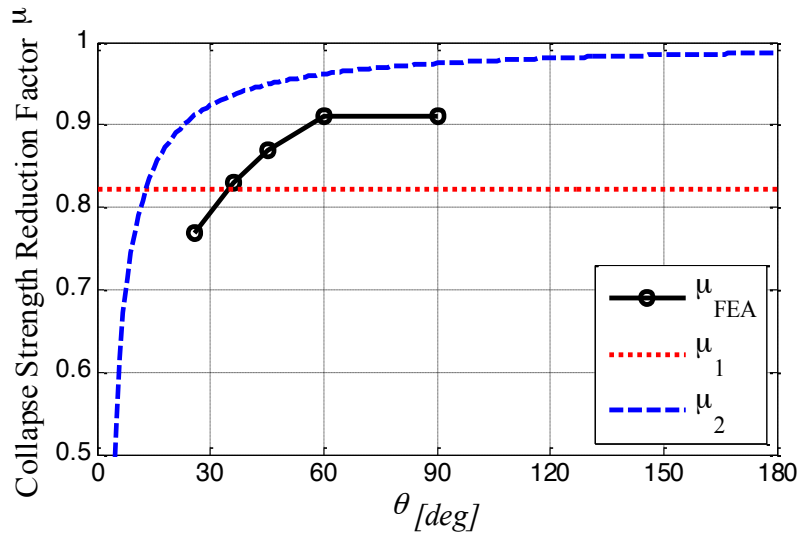
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[2] θ vs. μ



Collapse strength reduction factor μ is inversely proportional to θ .

Sensitivity Study of Collapse Strength Reduction Factor

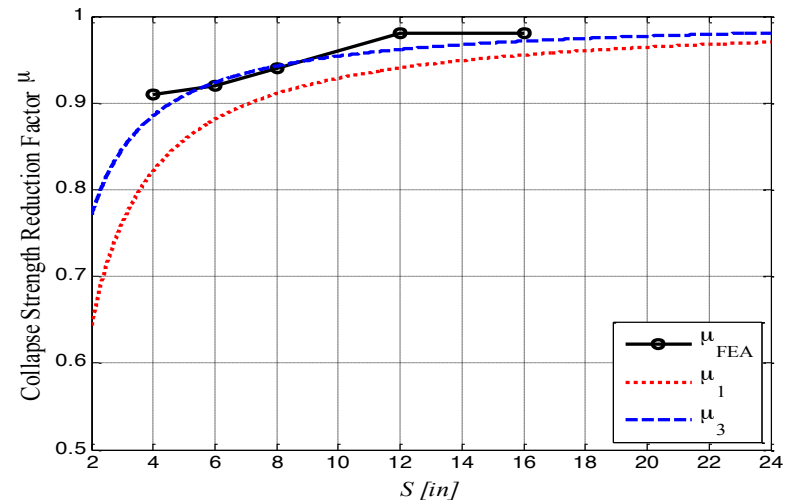
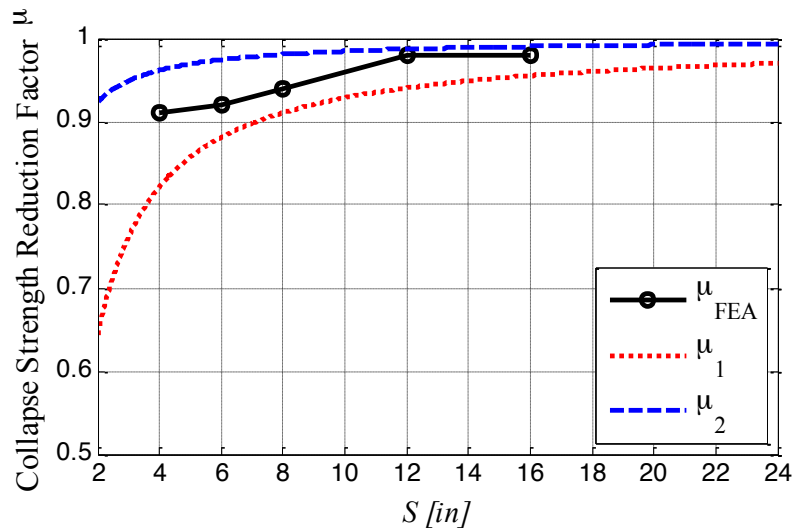
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[3] S vs. μ



Collapse strength reduction factor μ is inversely proportional to S .

Sensitivity Study of Collapse Strength Reduction Factor

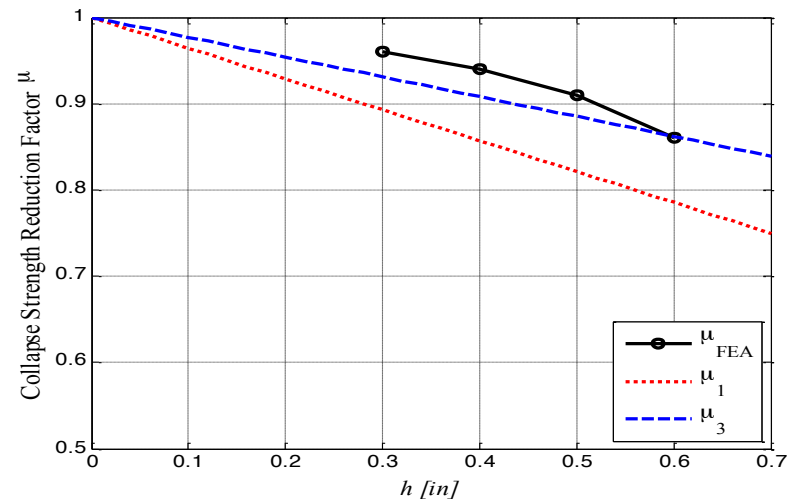
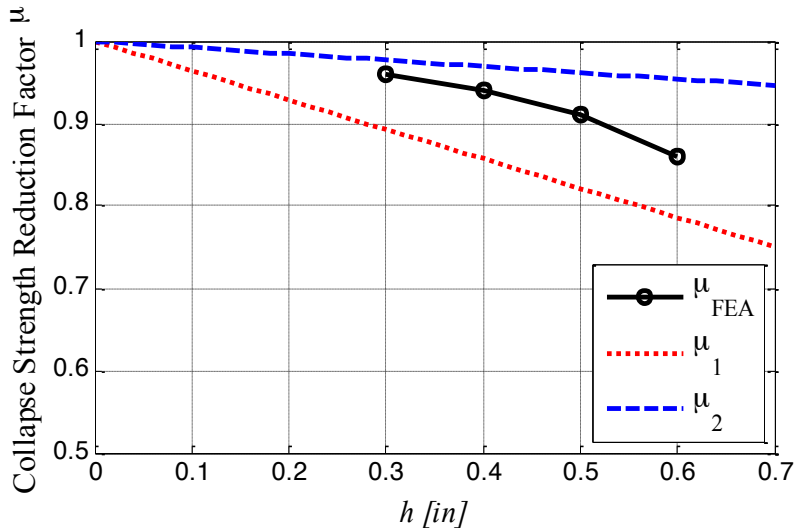
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[4] h vs. μ



Collapse strength reduction factor μ is “linearly” proportional to h .

Sensitivity Study of Collapse Strength Reduction Factor

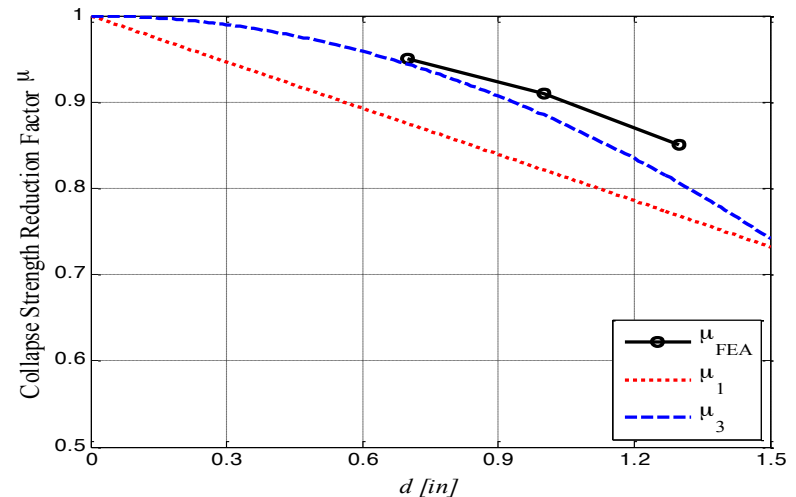
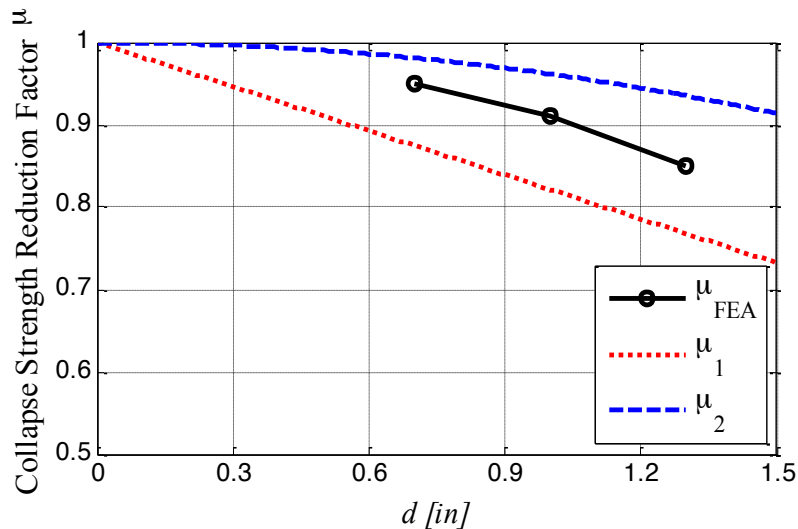
$$\mu_1 = 1 - \frac{d}{S} \cdot \frac{h}{t}$$

$$\mu_2 = 1 - 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_3 = 1 - 3 \cdot 90 \cdot \frac{d^2}{SD\theta} \cdot \frac{h}{t}$$

$$\mu_{\text{FEA}} = P_{\text{scallop}}^{\text{FEA}} / P_{\text{pipe}}^{\text{FEA}}$$

[5] d vs. μ



Collapse strength reduction factor μ is a quadratic function of d .

IV. Conclusions and Future Work

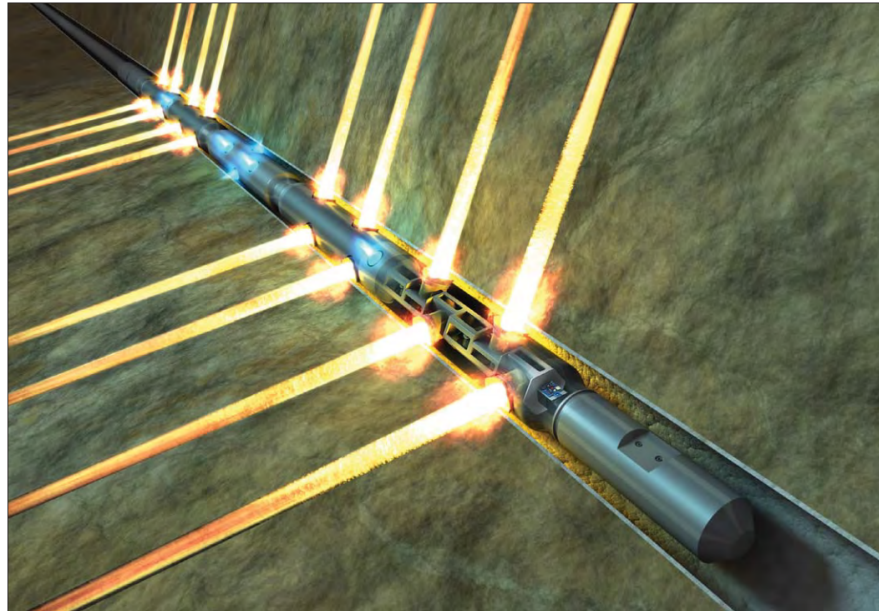
Conclusions and Future Work

- An analytical collapse strength equation based on Tamano formula was proposed for scalloped perforating guns.
- The proposed equation was thoroughly validated with the aid of FEA in a multivariable parametric space – an analysis hardly affordable with the use of physical tests.
- An FEA method used to validate the proposed equation showed strong agreement with the test data giving collapse predictions for scalloped tubulars within 5% of the test results.
- The method applied to scalloped perforating guns can also be used for any tubulars with patterned cutouts or recesses, such as prepacked sand screens, perforated or slotted liners, etc.



IPS-16-39

Questions?



Publications

- Zhao, H., Iblings, D., Barykin, A., and Mehdi, M., 2015, Plastic Collapse Behaviors of Tubulars with Recess Patterns, Proceedings of ASME International Mechanical Engineering Congress & Exposition, IMECE2015-50204, Houston, TX.
- Zhao, H., Iblings, D., Barykin, A., and Mehdi, M., 2016, Plastic Collapse Behaviors of Tubulars with Recess Patterns, ASCE-ASME Journal of Risk and Uncertainty in Engineering Systems, Part B: Mechanical Engineering, Accepted.